Do these converge or diverge? Justify

$$\sum_{k=0}^{\infty} \left(\frac{-1}{3} \right)^k$$

$$\sum_{k=1}^{\infty} \left(\frac{\cos(k\pi)}{\sqrt{k}} \right)$$

Do these converge or diverge? Justify

$$\sum_{k=0}^{\infty} \left(\frac{k^2}{k^3 + 2} \cdot \left(-1 \right)^k \right)$$

$$\sum_{k=0}^{\infty} \frac{k}{2^k} \cos(k\pi)$$

$$\sum_{k=1}^{\infty} \left(k \cdot \sin\left(\frac{1}{k}\right) \cdot \left(-1\right)^{k} \right)$$

$$\sum_{k=0}^{\infty} x^k$$

$$\sum_{k=1}^{\infty} \frac{\left(x-2\right)^k}{k}$$

$$\sum_{k=1}^{\infty} \frac{\left(x-3\right)^k}{k^2}$$

$$\sum_{n=1}^{\infty} \frac{\left(x+1\right)^n}{\sqrt{n}}$$

$$\sum_{n=0}^{\infty} \frac{x^{2n-1}}{2n-1} \left(-1\right)^n$$

$$\sum_{k=1}^{\infty} \frac{\left(x+1\right)^k}{3^k \cdot k}$$

Find the radius of convergence

$$\sum_{k=1}^{\infty} \frac{x^{2k}(k)!}{k^k}$$

Simplify

$$1-x^2+x^4-x^6+x^8+...$$

Estimate the following integral using series

$$\int_0^1 e^{\left(-\frac{x^2}{2}\right)} dx =$$

$$\int_0^1 \frac{1}{1+\sqrt{x}} dx$$

$$\int \frac{\sin(x)}{x} dx =$$

Write the first three terms of the Taylor polynomial for $\tan(x)$ evaluated around 45°. (Careful)

Write a Taylor series to approximate $Tan^{-1}(x^2)$

Use an infinite series to approximate $\sqrt{5}$

Use a McLaurin series to approximate ln(16)